

**Prof. Dr. Alfred Toth**

## **Semiotische Ränder und Nachbarschaften**

### **1. Definitionen**

#### **1.1. Grenzen**

$$G((3.a, 2.b, 1.c), (c.1, b.2, a.3)) = ((3.a, 2.b, 1.c) \cup (c.1, b.2, a.3)) \setminus ((3.a, 2.b, 1.c) \cap (c.1, b.2, a.3)).$$

#### **1.2. Ränder**

$$\mathcal{R}_\lambda(3.a, 2.b, 1.c) = (\{1.x\}, \{2.y\}, \{3.z\} \mid x < a, y < b, z < c)$$

$$\mathcal{R}_\rho(3.a, 2.b, 1.c) = (\{1.x\}, \{2.y\}, \{3.z\} \mid x > a, y > b, z > c)$$

$$\mathcal{R}_\lambda(c.1, b.2, a.3) = (\{x.1\}, \{y.2\}, \{z.3\} \mid x < c, y < b, z < a)$$

$$\mathcal{R}_\rho(c.1, b.2, a.3) = (\{x.1\}, \{y.2\}, \{z.3\} \mid x > c, y > b, z > a).$$

#### **1.3. Randgrenzen**

$$\mathfrak{G}_{ZTh\lambda} = G((3.a, 2.b, 1.c), (c.1, b.2, a.3)) \cap \mathcal{R}_\lambda(3.a, 2.b, 1.c)$$

$$\mathfrak{G}_{ZTh\rho} = ((3.a, 2.b, 1.c), (c.1, b.2, a.3)) \cap \mathcal{R}_\rho(3.a, 2.b, 1.c)$$

$$\mathfrak{G}_{RTh\lambda} = ((3.a, 2.b, 1.c), (c.1, b.2, a.3)) \cap \mathcal{R}_\lambda(c.1, b.2, a.3)$$

$$\mathfrak{G}_{RTh\rho} = ((3.a, 2.b, 1.c), (c.1, b.2, a.3)) \cap \mathcal{R}_\rho(c.1, b.2, a.3).$$

#### **1.4. Nachbarschaft**

$$N_\lambda(3.a, 2.b, 1.c) = (\{1.x\}, \{2.y\}, \{3.z\} \mid x < a, y < b, z < c) \cup \\ \{(1.\pm x), (2.\pm y), (3.\pm z)\}$$

$$N_\rho(3.a, 2.b, 1.c) = (\{1.x\}, \{2.y\}, \{3.z\} \mid x > a, y > b, z > c) \cup \\ \{(1.\pm x), (2.\pm y), (3.\pm z)\}$$

$$N_\lambda(c.1, b.2, a.3) = (\{x.1\}, \{y.2\}, \{z.3\} \mid x < c, y < b, z < a) \cup \\ \{(1.\pm x), (2.\pm y), (3.\pm z)\}$$

$$N_0(c.1, b.2, a.3) = (\{x.1\}, \{y.2\}, \{z.3\} \mid x > c, y > b, z > a) \cup \\ \{(1.\pm x), (2.\pm y), (3.\pm z)\}.$$

## 2. Beispiele

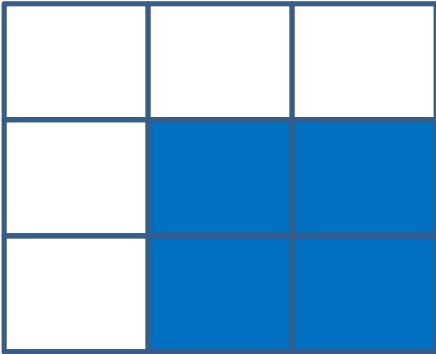
$$DS = [(3.1, 2.1, 1.3) \times (3.1, 1.2, 1.3)]$$



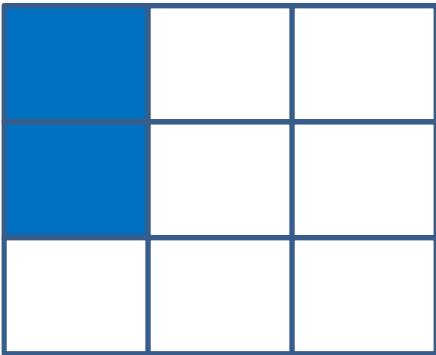
$$G((3.1, 2.1, 1.3), (3.1, 1.2, 1.3)) = (1.2, 2.1)$$


$$\mathcal{R}_\lambda(3.1, 2.1, 1.3) = (1.1, 1.2)$$

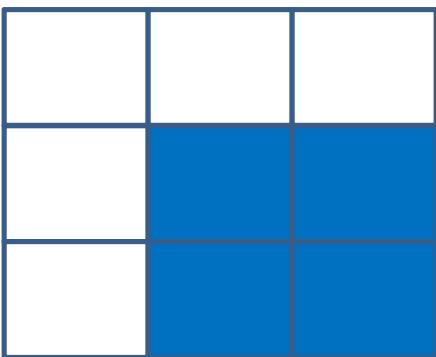

$$\mathcal{R}_\rho(3.1, 2.1, 1.3) = (3.2, 3.3, 2.2, 2.3)$$



$$\mathcal{R}_\lambda(3.1, 1.2, 1.3) = (1.1, 2.1)$$



$$\mathcal{R}_\rho(3.1, 1.2, 1.3) = (2.2, 3.2, 2.3, 3.3)$$

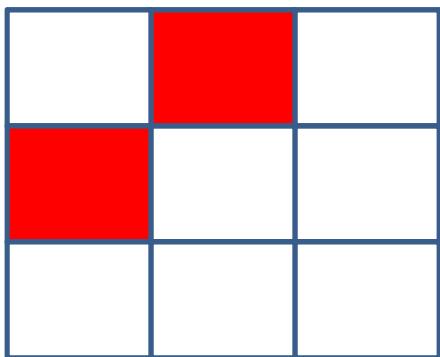


$$\mathfrak{G}_{ZTh\lambda} = G((3.1, 2.1, 1.3), (3.1, 1.2, 1.3)) \cap \mathcal{R}_\lambda(3.1, 2.1, 1.3) = (1.2)$$

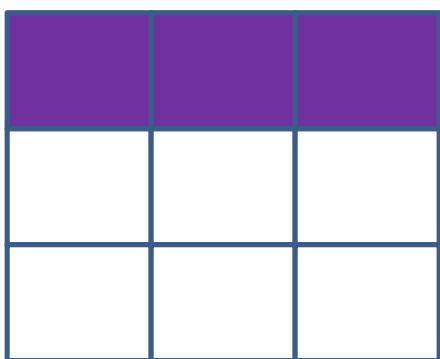
$$\mathfrak{G}_{ZTh\rho} = G((3.1, 2.1, 1.3), (3.1, 1.2, 1.3)) \cap \mathcal{R}_\rho(3.1, 2.1, 1.3) = \emptyset$$

$$\mathfrak{G}_{RTh\lambda} = G((3.1, 2.1, 1.3), (3.1, 1.2, 1.3)) \cap \mathcal{R}_\lambda(3.1, 1.2, 1.3) = (2.1)$$

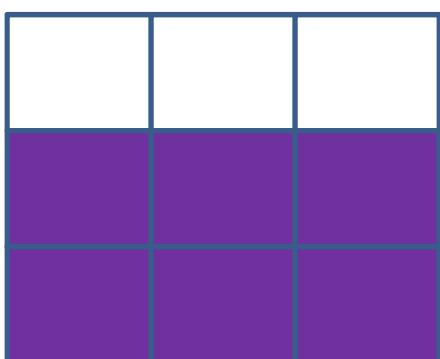
$$\mathfrak{G}_{RTh\rho} = G((3.1, 2.1, 1.3), (3.1, 1.2, 1.3)) \cap \mathcal{R}_\rho(3.1, 1.2, 1.3) = \emptyset.$$



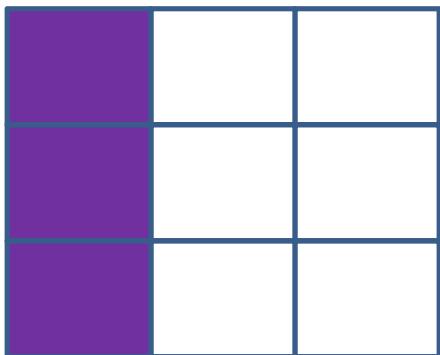
$$N_\lambda(3.1, 2.1, 1.3) = (1.1, 1.2, 1.3)$$



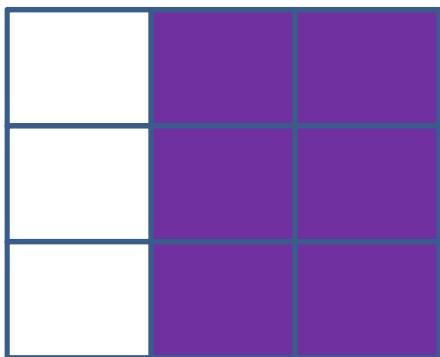
$$N_\rho(3.1, 2.1, 1.3) = (2.1, 2.2, 2.3, 3.1, 3.2, 3.3)$$



$$N_\lambda(3.1, 1.2, 1.3) = (1.1, 2.1, 3.1)$$



$$N_\rho(3.1, 1.2, 1.3) = (1.2, 1.3, 2.2, 2.3, 3.2, 3.3)$$



## Literatur

Toth, Alfred, Die Ränder von Zeichen und Objekten. In: Electronic Journal for Mathematical Semiotics 2013a

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Toth, Alfred, Semiotisch-ontische Äquivalenz von Grenzen und Rändern. In: Electronic Journal for Mathematical Semiotics, 2013c

Toth, Alfred, Semiotisch-ontische Äquivalenz eingebetteter Teilsysteme. In: Electronic Journal for Mathematical Semiotics, 2013d

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