

Semiotische Ränder und Nachbarschaften

1. Definitionen

1.1. Grenzen

$$G((3.a, 2.b, 1.c), (c.1, b.2, a.3)) = ((3.a, 2.b, 1.c) \cup (c.1, b.2, a.3)) \setminus ((3.a, 2.b, 1.c) \cap (c.1, b.2, a.3)).$$

1.2. Ränder

$$\mathcal{R}_\lambda(3.a, 2.b, 1.c) = (\{1.x\}, \{2.y\}, \{3.z\} \mid x < a, y < b, z < c)$$

$$\mathcal{R}_\rho(3.a, 2.b, 1.c) = (\{1.x\}, \{2.y\}, \{3.z\} \mid x > a, y > b, z > c)$$

$$\mathcal{R}_\lambda(c.1, b.2, a.3) = (\{x.1\}, \{y.2\}, \{z.3\} \mid x < c, y < b, z < a)$$

$$\mathcal{R}_\rho(c.1, b.2, a.3) = (\{x.1\}, \{y.2\}, \{z.3\} \mid x > c, y > b, z > a).$$

1.3. Randgrenzen

$$\mathfrak{G}_{ZTh\lambda} = G((3.a, 2.b, 1.c), (c.1, b.2, a.3)) \cap \mathcal{R}_\lambda(3.a, 2.b, 1.c)$$

$$\mathfrak{G}_{ZTh\rho} = ((3.a, 2.b, 1.c), (c.1, b.2, a.3)) \cap \mathcal{R}_\rho(3.a, 2.b, 1.c)$$

$$\mathfrak{G}_{RTh\lambda} = ((3.a, 2.b, 1.c), (c.1, b.2, a.3)) \cap \mathcal{R}_\lambda(c.1, b.2, a.3)$$

$$\mathfrak{G}_{RTh\rho} = ((3.a, 2.b, 1.c), (c.1, b.2, a.3)) \cap \mathcal{R}_\rho(c.1, b.2, a.3).$$

1.4. Nachbarschaft

$$N_\lambda(3.a, 2.b, 1.c) = (\{1.x\}, \{2.y\}, \{3.z\} \mid x < a, y < b, z < c) \cup \{(1.\pm x), (2.\pm y), (3.\pm z)\}$$

$$N_\rho(3.a, 2.b, 1.c) = (\{1.x\}, \{2.y\}, \{3.z\} \mid x > a, y > b, z > c) \cup \{(1.\pm x), (2.\pm y), (3.\pm z)\}$$

$$N_\lambda(c.1, b.2, a.3) = (\{x.1\}, \{y.2\}, \{z.3\} \mid x < c, y < b, z < a) \cup \{(1.\pm x), (2.\pm y), (3.\pm z)\}$$

$$N_p(c.1, b.2, a.3) = (\{x.1\}, \{y.2\}, \{z.3\} \mid x > c, y > b, z > a) \cup \{(1.\pm x), (2.\pm y), (3.\pm z)\}.$$

2. Beispiele

$$DS = [(3.1, 2.1, 1.3) \times (3.1, 1.2, 1.3)]$$

$$G((3.1, 2.1, 1.3), (3.1, 1.2, 1.3)) = (1.2, 2.1)$$

$$\mathcal{R}_\lambda(3.1, 2.1, 1.3) = (1.1, 1.2)$$

$$\mathcal{R}_\rho(3.1, 2.1, 1.3) = (3.2, 3.3, 2.2, 2.3)$$

$$\mathcal{R}_\lambda(3.1, 1.2, 1.3) = (1.1, 2.1)$$

$$\mathcal{R}_\rho(3.1, 1.2, 1.3) = (2.2, 3.2, 2.3, 3.3)$$

$$\mathfrak{G}_{\text{ZTh}\lambda} = G((3.1, 2.1, 1.3), (3.1, 1.2, 1.3)) \cap \mathcal{R}_\lambda(3.1, 2.1, 1.3) = (1.2)$$

$$\mathfrak{G}_{\text{ZTh}\rho} = G((3.1, 2.1, 1.3), (3.1, 1.2, 1.3)) \cap \mathcal{R}_\rho(3.1, 2.1, 1.3) = \emptyset$$

$$\mathfrak{G}_{\text{RTh}\lambda} = G((3.1, 2.1, 1.3), (3.1, 1.2, 1.3)) \cap \mathcal{R}_\lambda(3.1, 1.2, 1.3) = (2.1)$$

$$\mathfrak{G}_{\text{RTh}\rho} = G((3.1, 2.1, 1.3), (3.1, 1.2, 1.3)) \cap \mathcal{R}_\rho(3.1, 1.2, 1.3) = \emptyset.$$

$$N_{\lambda}(3.1, 2.1, 1.3) = (1.1, 1.2, 1.3)$$

$$N_{\rho}(3.1, 2.1, 1.3) = (2.1, 2.2, 2.3, 3.1, 3.2, 3.3)$$

$$N_\lambda(3.1, 1.2, 1.3) = (1.1, 2.1, 3.1)$$

$$N_\rho(3.1, 1.2, 1.3) = (1.2, 1.3, 2.2, 2.3, 3.2, 3.3)$$

Literatur

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